## 10 Fast Evolutionary Learning in the SOM

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Above we dealt with vector-valued  $\mathbf{x}(t)$  and  $\mathbf{m}_i(t)$ . The SOM philosophy, however, can be much more general. The structures of the models and data can be different: it will suffice that some fitness function is definable between the general inputs X and the general models  $M_i$ , respectively. Let this function be denoted  $f(X, M_i)$ . Notice carefully that we do not need any distance function in the X space, nor in the  $M_i$  space.

Even under the above conditions, the SOM can be computed in an "evolutionary" process (cf. [1], Sec. 5.7). We may initialize the models as random samples from the set of possible models. Next we input the samples of X, one at a time, and at each step determine that model  $M_c$  for which

$$c = \arg\max_{i} \{ f(X, M_i) \} . \tag{77}$$

The next step is some kind of variation of the  $M_i$  in the neighborhood set  $N_c$  of the fittest model  $M_c$ . This variation usually means random but statistically independent replacement of each  $M_i$ ,  $i \in N_c$  by some other possible model M on the condition  $f(X, M) > f(X, M_i)$ .

The evolutionary learning can be implemented by the batch-type SOM without random probing, whereupon it proceeds fast:

- 1. Initialize the models  $M_i$ , e.g., by a random choice of their parameter values from a set of possible values.
- 2. Input a number of items X and list each of them under the respective winner unit (i.e. that  $M_i$  for which some fitness function  $f(X, M_i)$  is maximum). In case there is a tie, i.e., two or more  $M_i$  have the same fitness to X, select one of them randomly for the effective unique "winner" under which the listing is made.
- 3. Find a new value  $M'_i$  for each  $M_i$  such that if  $U_i$  is the union of lists relating to model  $M_i$  in the same way as in the Batch Map algorithm discussed in Sec. 1, the sum of the fitness-function values  $f(X, M'_i)$ ,  $X \subset U_i$  is increased. If there exist ties, a random choice between the best  $M'_i$  is made.
- 4. Repeat from step 2.

## References

- [1] T. Kohonen, Self-Organizing Maps, Springer-Verlag, Berlin, 1995; 2nd edition, 1997.
- [2] T. Kohonen, Fast evolutionary learning with batch-type self-organizing maps. To appear in *Neural Processing Letters*, 1999.