Discrete-Time Signals and Systems Time-Domain Representations of Discrete-Time Signals and Systems
Time-domain representation of a discrete-time signal as a sequence of numbers
Basic sequences and operations on sequences
Discrete-time systems in processing of discrete-time signals
Linear and time-invariant systems

















































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• An important subclass of LTI discrete-time is characterized by a linear constant coefficient difference equation

$$\sum_{k=0}^{N} d_{k} y[n-k] = \sum_{k=0}^{M} p_{k} x[n-k]$$

where x[n] and y[n] are, respectively, the input and output of the system and  $\{d_k\}$  and  $\{p_k\}$  are constants

• The *order* of the system is given by max{*N,M*}

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# Classification Based on Output Calculation Process

- If the output sample can be calculated sequentially, knowing only the present and past input samples, the filter is said to be *nonrecursive* discrete-time system
- If, on the other hand, the computation of the output involves past output samples in addition to the present and past input samples, the filter is known as *recursive* discrete-time system

$$y[n] = -\sum_{k=1}^{N} \frac{d_k}{d_0} y[n-k] + \sum_{k=0}^{M} \frac{p_k}{d_0} x[n-k]$$
  
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• The simplest model is described by the inputoutput relation

 $y[n] = \sum_{k=0}^{M} p_k x[n-k]$ 

- A moving average (MA) model is an FIR discrete-time system
- It can be considered as a generalization of the *M*-point moving average filter with different weights assigned to input samples

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Correlation of Signals and Matched Filters

# Correlation of Signals

• There are applications where it is necessary to compare one reference signal with one or more signals to determine the similarity between the pair and to determine additional information based on the similarity

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#### Definitions

 A measure of similarity between a pair of energy signals, x[n] and y[n], is given by the crosscorrelation sequence r<sub>xy</sub>[l] defined by

$$r_{xy}[l] = \sum_{n=1}^{\infty} x[n]y[n-l], \quad l = 0, \pm 1, \pm 2, ...$$

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• The parameter *l* called *lag*, indicates the time-shift between the pair of signals











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