

## T-61.140 Signal Processing Systems

2nd mid term exam, Fri 3.5.2002 12-15 M (Simula, Parviainen)

You may use a graphical calculator of your own. There are formulae on accompanying papers - use them!

- 1) (0-3p) Answer, if the statement is true (T) or false (F). Correct answer +1p, wrong -1p, no answer 0p. Explain briefly!

**ATT!** There are four statements, max points 3.

- Convolution of input signal and impulse response in time-domain corresponds the sum of frequency response and Fourier-transform of input signal.
- Given amplitude spectrum  $|X(e^{j\omega})|$  of any signal  $x[n]$ , it is possible to recover time-domain sequence  $x[n]$  from amplitude spectrum, if there is enough calculation power in the computer.
- If  $h_{lp}[n]$  is impulse response of a low pass filter, then a high pass filter  $h_{hp}[n]$  can be obtained by multiplying  $h_{lp}[n]$  with  $(-1)^n$ .
- Continuous-time Fourier-transform is periodic with the period of  $2\pi$ .

- 2) (3p) Answer with a few sentences.

- What do terms analog(ue), discrete and digital signal mean?
- Why is it useful to process signal digitally?

- 3) (6p) LTI system is defined with a difference equation

$$y[n] = 0.25 x[n] - 0.5 x[n-1] + 0.25 x[n-2]$$

- (1p) Draw the block (flow) diagram of LTI system.
- (2p) What is the frequency response of  $H(e^{j\omega})$ ?
- (1p) Sketch  $|H(e^{j\omega})|$  in range  $0.. \pi$ . Is the system of type lowpass / highpass / bandpass / bandstop?
- (2p) Compute the output  $y[n]$ , when the input is  $x[n] = \{0, 1, 1, 2, 1, 8, 2, 1, 1\}$ . Draw both  $x[n]$  and the filtered  $y[n]$ .

- 4) (6p) Consider a continuous-time signal  $x(t)$ , which consists of three cosine components (150 Hz, 350 Hz, 450 Hz)

$$x(t) = \cos(2\pi 150 t) + \cos(2\pi 350 t) + \cos(2\pi 450 t)$$

- (2p) Sketch the spectrum  $|X(j\omega)|$  in range  $0..1500$  Hz.
- (1p) What is the lowest sampling frequency, with which there is no aliasing?
- (3p) Demonstrate the effect of too low sampling frequency in the spectrum of discrete-time signal  $|X(e^{j\omega})|$ . Choose the sampling frequency between  $350 < f_s < 450$ .

Turn!

5) (6p) **Reply to either A or B.**

5A) The calculator of the assistant is broken. You should help him and produce a sequence of squares  $\{\dots, 0, 1, 4, 9, 16, 25, \dots\}$  using a third order recursive LTI filter (allowed operations: sum of signals, amplification of constants, delay). Figure out or compute the coefficients of the filter and determine the initial values of delay registers.

Hints:

- Examine  $y[n] = n^2$ ,  $y[n - k] = (n - k)^2$
- Examine sequences  $\{0, 1, 4, 9, 16, 25, \dots\}$ ,  
 $\{(1 - 0), (4 - 1), (9 - 4), (16 - 9), (25 - 16), \dots\}$ ,  
 $\{(4 - 1) - (1 - 0), (9 - 4) - (4 - 1), (16 - 9) - (9 - 4), (25 - 16) - (16 - 9), \dots\}$
- Keep the input always as zero ( $x[n] \equiv 0$ , for all  $n$ ).

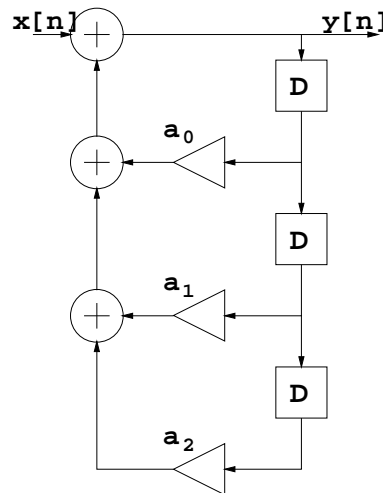


Figure 1: Recursive third order IIR filter (without FIR part).

5B) In the study program 2001-2002 there is a keyword “frequency analysis of signals” in the contents of T-61.140 Signal Processing Systems. Write down an essay on this subject. The maximum length of the essay is two pages with line space of two; illustrations can be drawn to clarify the text.